## 13-1A Trigonometric Identities

Trigonometric Identity: an equation involving trigonometric functions that is true for all values for which every expression in the equation is defined.

| Trigonometric Identities |  |  |
| :---: | :--- | :--- |
| Quotient Identities |  |  |
| Reciprocal Identities |  |  |
| Pythagorean Identities |  |  |
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Trigonometric Identities - prove it! Quotient Identities


$$
\tan \theta=\frac{\sin \theta}{\cos \theta} \quad \cot \theta=\frac{\cos \theta}{\sin \theta}
$$

Trigonometric Identities - prove it! Reciprocal Identities
$\csc \theta=\frac{1}{\sin \theta}$
$\sec \theta=\frac{1}{\cos \theta}$
$\cot \theta=\frac{1}{\tan \theta}$

Trigonometric Identities - prove it! Pythagorean Identities
$\cos ^{2} \theta+\sin ^{2} \theta=1$
$\tan ^{2} \theta+1=\sec ^{2} \theta$

$\cot ^{2} \theta+1=\csc ^{2} \theta$

Using trig. identities to find a value

1. Find $\tan \theta$ if $\sec \theta=-2$ and $180^{\circ}<\theta<270^{\circ}$
2. Find $\sin \theta$ if $\cos \theta=1 / 2$ and $270^{\circ}<\theta<360^{\circ}$
3. Find $\csc \theta$ if $\cos \theta=2 / 3$ and $90^{\circ}<\theta<270^{\circ}$

How to use trigonometric identities to find exact trig. values

- Determine which trig. identity/identities to use.
- Use the trig. identity/identities as formulas.
- Use substitution and solve.
- Determine the sign of the trig. value based on the quadrant.

