

# 5-1 Operations with Polynomials

- multiply, divide, and simplify monomials and expressions involving powers.
- add, subtract, and multiply polynomials
- A.APR.1

**monomial**: an expression that is a **number**, a **variable**, or the **product of numbers and variables**.

<u>monomials</u>	<u>not monomials</u>
$x$ $5$ $5x$ $x^2yz$ $\frac{x}{5} = \frac{1}{5}x$	$x+5$ $x-5$  $\frac{x}{4}$

**constants**: monomials that contain no variables.

**coefficient**: the numerical factor of the monomial.

**degree**: the sum of the exponents of its variables.

- degree of non-zero constants is zero.
- zero does not have a degree.

monomial	coefficient	variable(s)	exponent(s)	degree
$1m$	1	$m$	1	1
$-7a^2$	-7	$a$	2	2
$x^3y^2$	1	$xy$	3, 2	5
$-4$	-4	—	—	0
$\frac{n^3p^4r}{3}$	$\frac{1}{3}$	$n, p, r$	3, 4, 1	8

$\frac{3 \ 4 \ r}{n \ p}$   
 $\frac{1}{3}$

## Property of Powers

Property	Definition	Example
Product of Powers	$a^m \cdot a^n = a^{m+n}$	$X^2 \cdot X^3 = X^{2+3} = X^5$ $X \cdot X \cdot X \cdot X \cdot X = X^5$
Quotient of Powers	$\frac{a^m}{a^n} = a^{m-n}$	$\frac{X^5}{X^2} = X^{5-2} = X^3$ <del><math>\frac{X \cdot X \cdot X \cdot X \cdot X}{X \cdot X}</math></del>
Power of a Power	$(a^m)^n = a^{m \cdot n}$	$(X^3)^2 = X^6$ $X^3 \cdot X^3$ $X^6$
Power of a Product	$(a^m b^n)^p = a^{mp} b^{np}$	$(X^2 Y^3)^4 = X^8 Y^{12}$
Power of a Quotient	$\left(\frac{a}{b}\right)^p = \frac{a^p}{b^p}$	$\left(\frac{X^3}{Y^2}\right)^2 = \frac{X^6}{Y^4}$
Negative Power	$X^{-m} = \frac{1}{X^m}$ $a^{-m} = \frac{1}{a^m}$	$\frac{X^2}{X^5} = X^{-3} = \frac{1}{X^3}$ <del><math>\frac{X \cdot X}{X \cdot X \cdot X \cdot X \cdot X}</math></del>
Zero Power	$a^0 = 1$	$\left(\frac{X^2}{Y^3}\right)^0 = \frac{(X^2)^0}{Y^3} = \frac{1}{Y^3}$

$10^2 = 100$   
 $10^1 = 10$   
 $10^0 = 1$   
 $10^{-1} = \frac{1}{10}$   
 $10^{-2} = \frac{1}{100}$

$0-9$   
 $1234567890$

### Simplifying Monomials:

- no powers of powers  $(X^3)^2 = X^6$
- each base appears exactly once  
 $(2x)(3x^2y) = 6x^3y$
- fractions are in simplest form  $\frac{X^4 Y^3}{X Y^2} = \frac{X^3 Y^2}{1}$
- no negative exponents

$\frac{\left(\frac{2}{3}\right)^{-3}}{\left(\frac{3}{2}\right)^{-3}} = \frac{2^{-3}}{3^{-3}} = \frac{3^3}{2^3} = \frac{27}{8}$

$\frac{a^{-3} b^4}{a^1 b^{-2}} = \frac{b^4 b^2}{a^3 a} = \frac{b^6}{a^4}$

Examples: Simplify.

1.  $(a^{-3})(a^2b^4)(c^{-1})$

$$a^{-1}b^4c^{-1}$$

$$\frac{b^4}{ac}$$

$$\frac{a^2b^4}{ac}$$

2.  $\frac{n^2}{n^{10}}$

$$n^{2-10} = n^{-8} = \frac{1}{n^8}$$

$$\frac{9a^6}{b^8}$$

3.  $\left(\frac{3a^3}{b^4}\right)^2$

$$\left(\frac{3a^3}{b^4}\right)\left(\frac{3a^3}{b^4}\right)$$

$$\frac{3 \cdot 3 a^3 a^3}{b^4 b^4} = \frac{9a^6}{b^8}$$

## 5-2 Polynomials

- adding and subtracting polynomials
- multiplying polynomials
- No CCSS

previous assignment:  
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**polynomial**: a monomial or a sum or difference of monomials.

<u>polynomials</u>	<u>not polynomials</u>
$x+5$ $x^2-3x+7$	$\frac{x}{y}$ $\sqrt{x} = x^{1/2}$

*terms*: the monomials that make up the polynomials.

*like terms*: same variables raised to the same degree.

*binomial*: made up of two terms.

*trinomial*: made up of three terms.

*degree of polynomials*: the highest degree of the monomial within the polynomial.

Examples: Determine whether or not the following are polynomials, then determine its degree.

1.  $c^4 - 4\sqrt{c} + 18$

not a poly

2.  $-16p^5 + \frac{3p^9q^7}{4}$

degree: 9

3.  $\frac{x}{z} + y^2$

not a poly

4.  $-2x^3 + 4x^2y^3 - 8xz$

degree: 5

## Adding and Subtracting Polynomials

- add or subtract the coefficients of the like terms.
- exponents of the variables remain the same.

Examples: Add or subtract the following polynomials.

1)  $(2a^3 + 5a - 7) + (a^3 - 3a + 2)$

$$2a^3 + 5a - 7 + a^3 - 3a + 2$$

$$3a^3 + 2a - 5$$

2)  $(3x^2 - 2x + 3) - (x^2 + 4x - 2)$

$$3x^2 - 2x + 3 - x^2 - 4x + 2$$

$$2x^2 - 6x + 5$$

## Multiplying Polynomials - distributive property

- multiply the coefficients, multiply the variables (add the exponents)
- combine like terms, if necessary.

Examples:

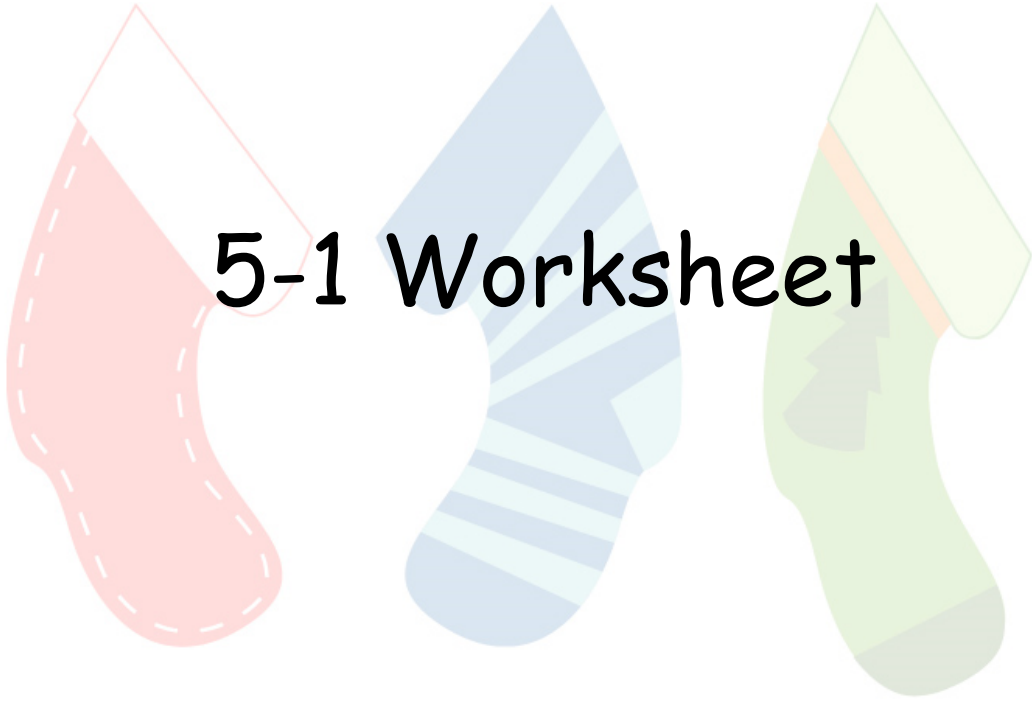
1.  $y(4y^2 + 2y - 3)$

2.  $3x(2x^2y - 5x^3y^2)$

$$6x^3y - 15x^4y^2$$

3.  $(a + 2)(a^2 - 3a + 5)$

$$\begin{array}{r} a^3 - 3a^2 + 5a \\ + 2a^2 - 6a + 10 \\ \hline a^3 - a^2 - a + 10 \end{array}$$



# 5-1 Worksheet