

6-2 Inverse Functions & Relations

relations: set of ordered pairs.

domain: set of all 1st coordinates in a relation. *x, input, independent*

range: set of all 2nd coordinates in a relation. *y, output, dependent*

inverse relation: a relation where the domain and range values are reversed.

(y, x)

y

x

$(5, 200)$

$(10, 200)$

function: a relation whose domain does not repeat.

Example: $R = \{(1, 2), (3, 4), (5, 6)\}$

domain: $\{1, 3, 5\}$

range: $\{2, 4, 6\}$

inverse: $\{(2, 1), (4, 3), (6, 5)\}$

Is the relation a function? *yes*

Is the inverse a function? *yes*

$$\begin{aligned}
 f \circ g &= 2(4x+3) - (4x+3) + 1 \\
 &= 2(16x^2 + 24x + 9) - 4x - 3 + 1 \\
 &= 32x^2 + 48x + 18 - 4x - 2 \\
 &= 32x^2 + 44x + 16
 \end{aligned}$$

~~$$16x^2 + 9$$~~

Definition of Inverse Functions: Two functions are inverse functions **IFF** both of their compositions are the identity function. That is, if $f(x)$ and $g(x)$ represent functions, then f and g are inverses **IFF**

$$f \circ g(x) = x \quad \text{and} \quad g \circ f(x) = x$$

- denoted by f^{-1} , which reads "f inverse" or "the inverse of f"
- not all inverses are functions, they are then called inverse relations.

$$f^{-1}(x)$$

$$2^{-1} = \frac{1}{2}$$

Example: Determine whether the following functions are inverses of each other.

$$h(x) = 2x + 8$$

$$g(x) = \frac{x-8}{2}$$

$$h \circ g$$

$$h(g(x))$$

$$h\left(\frac{x-8}{2}\right) = 2\left(\frac{x-8}{2}\right) + 8$$

$$g \circ h = g(h(x))$$

$$g(2x+8) = \frac{2x+8-8}{2}$$

$$h \circ g = x$$

$$h \circ g = x$$

yes, inverses

$$g \circ h = \frac{2x}{2}$$

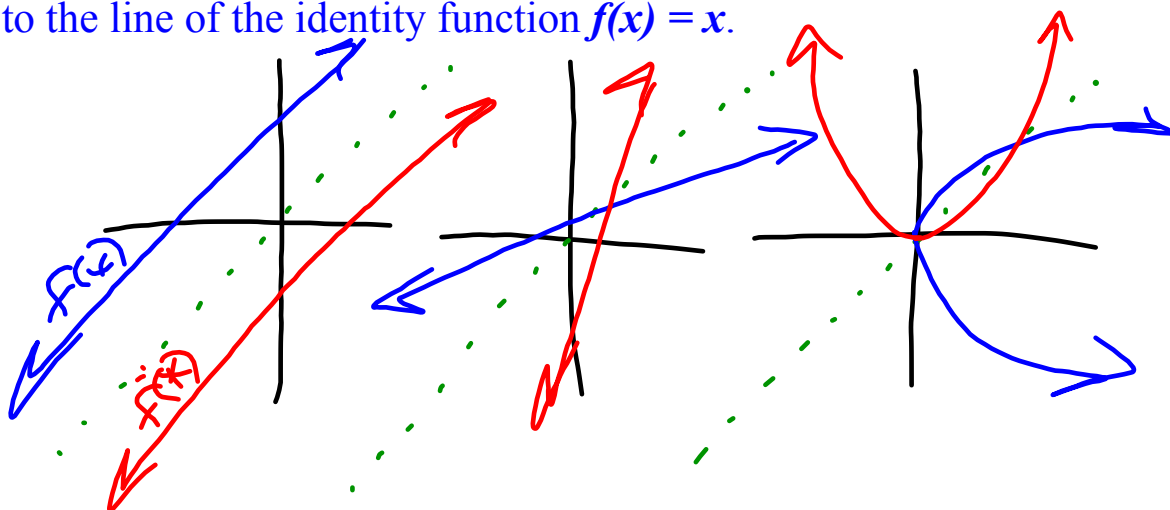
$$g \circ h = x$$

To find an inverse function:

- replace $f(x)$ with y .
- interchange the x and y variables.
- solve for the *new* y .
- check your answer by compositions or by graphing.

$$\frac{f(x)}{\underbrace{\quad}} \quad (y, x)$$

The graphs of all **functions** and their **inverses** are symmetrical to the line of the identity function $f(x) = x$.



Determine the inverse function of $f(x) = 2x + 3$. Then graph the function and its inverse.

$$y = 2x + 3$$

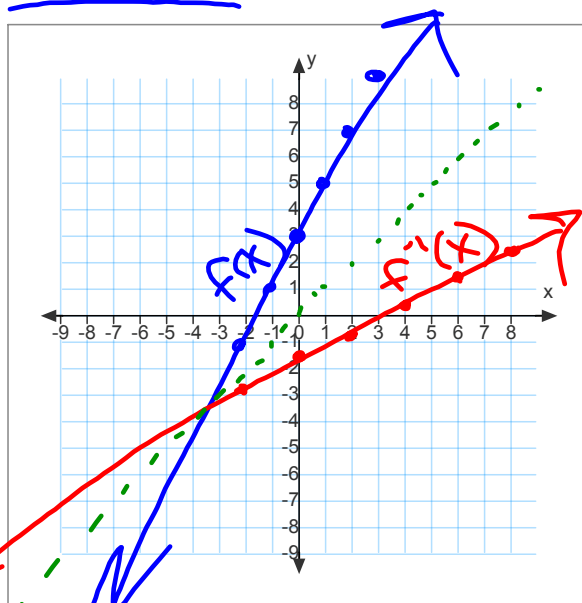
$$x = 2y + 3$$

$$2y + 3 = x$$

$$2y = x - 3$$

$$y = \frac{x}{2} - \frac{3}{2}$$

$$f^{-1}(x) = \frac{1}{2}x - \frac{3}{2}$$



$$y = x$$

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Attachments

7-7 HW.notebook