

7-3B Evaluating Logarithmic Expressions

- evaluate logarithmic expressions without a calculator

Evaluating Logarithmic Functions

- rewrite in exponential form: $x = by$
- create common bases and solve for y.

If $\underline{b}^m = \underline{b}^n$, $m = n$.

Evaluate.

1. $\log_3 243$

$$3^? = 243$$

$$3^y = 3^5$$

$$y = 5$$

$$\log_3 243$$

$$\log_3 3^5$$

$$5$$

$$\sqrt{5^2}$$

$$(\sqrt{3})^5$$

2. $\log_2 \frac{1}{8}$

$$2^? = \frac{1}{8}$$

$$2^y = \frac{1}{2^3}$$

$$2^y = 2^{-3}$$

$$-3$$

$$\log_2 2^{-3}$$

$$\log_5 5^7 = 7$$

$$\sqrt[4]{6} \quad \sqrt[2]{8}$$

3. $\log_9 3$

$$9^? = 3$$

$$(3^2)^y = 3^1$$

$$3^{2y} = 3^1$$

$$2y = 1$$

$$y = \frac{1}{2}$$

Since $y = b^x$ and $y = \log_b x$ are inverses of each other, they "undo" each other.

- ~~$b^{\log_b x} = x$~~ ex: ~~$2^{\log_2 8} = 8$~~
(an exponential written with a log as the exponent)

$\log_2 8$
 $2^3 = 8$
 $2^? = 8$
 $\log_2 8 = 3$

- ~~$\log_b b^x = x$~~ ex: ~~$\log_3 3^7 = 7$~~
(a logarithm of a power with same base as the logarithm)

$\log_3(3^?)$

$3^? = 3^7$

~~$\log_7 7^5$~~

~~$\log_3 3^4$~~

p. 472
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